Positive Ricci Curvature through Cheeger deformation

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Abstract. Let (M, g) be a Riemannian manifold with an isometric *G*-action. If a principal orbit has finite fundamental group and $\operatorname{Ricci}_{M^{reg}/G} \geq 1$, Searle–Wilhelm proved that *M* admits a new metric \tilde{g} of positive Ricci curvature. \tilde{g} is obtained after a conformal change followed by a Cheeger deformation. The question remained on whether it is sufficient to consider only the Cheeger deformation to attain positive Ricci curvature on the new metric \tilde{g} . Here we approach this question by giving necessary and sufficient conditions on the *G*-action. In particular, we construct an infinite family of manifolds satisfying the hypothesis of Searle–Wilhelm that do not develop positive Ricci curvature after Cheeger deformation. Moreover, as a byproduct of the theory, we give simpler proofs to Searle–Wilhelm result and to Lawson–Yau theorem on the existence of positive scalar curvature on manifolds with nonabelian symmetry.